Determining the Best Fleet Sizing of a Container Terminal for a Given Layout

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Abstract

Container handing sea Ports are the hearts many supply chains which are dependent on exports and imports. The overall operations productivity of the container terminals (CT) directly links with the efficiency of the supply chains. Normally in CTs inward and outward containers from/to vassals are handled in two different cycles as unloading and loading. Once a ship arrives to the berth, unloading will take place first and this is followed by the loading operations. In order to handle these activities, three types of equipments are used: Query Carne (QC) is used for (un)loading containers from a ship, Prime movers are used to move containers from/to QC to yard or vice versa. Yard cranes are used to (un)load to/from yard. Since number of different equipments operating in a constraint environment this leads to traffic congestions at buffer zones, intersections of the route network of the terminal etc. Due to these phenomena overall efficiency of the terminal reduces. Therefore, this research is focused on determining the most effective layout arrangement and respective fleet size of prime movers by considering external and internal aspects of a given CT. This problem is modelled and solved in analytically and tested in Arena simulated environment. The proposed approach is able to minimize idle times of CT equipments and minimize resources consumption.

Keywords
Container terminal operations, productivity, fleet sizing, simulation with Arena

1. Introduction

Container trade worldwide has grown 9.5% per year during the last decade and will continue with the growth rate of 8% in the coming years (Lu Chen, 2007). Responding to this demand increase in containerization, in ports point of view, is important to enhance the levels of services. It could only be done by handling materials (containers) more efficient ways in side of the port. It is because; a port’s efficiency is often measured in terms of its throughput and typical ship turnaround time (i.e. a ship’s time at berth plus any delay caused by the port). Container terminal is the facility in port where all the material handling activities are been carried out. Daily various types of cargos and vassals ships come to the port and so to container terminal, the allocation of those to certain berths in the CT is done according to a certain priority level. Unloading and loading of containers is done using quay cranes (QC). At the storage blocks in the yard, yard cranes (YCs) carry out a number of operations that include lifting and placing. Yard vehicles are used for transporting containers between and quayside and the yard, servicing both quay cranes and yard cranes as prime movers. Once they have transported to the stacking area unloading and placing is done by stacking cranes and lifting vehicles.

There are many factors that affect the operational efficiency of a Container Terminal. Basically the efficiency of the Container Terminal depends on the layout configuration which provides high performance of the material handling equipments, proper arrangement of buffer zone, optimum traffic route, usage of optimal number of prime movers etc.
Crane clashing and collation of prime movers also can be minimized with a proper Container Terminal layout. There are number of decision problems such as the design of storage policies in the yard according to the specific requirements of the container (size, weight, destination, export/import etc.), allocation of containers to prime movers, routing and scheduling of yard cranes, the design of re-marshalling policies for export containers in order to achieve a proper layout configuration. Number of researches has done in recent past [1-4] with respect to CT operations. However, it is rare to find many researches linking layout configuration and optimal fleet sizes with overall operational efficiency of CT. However, some works involved to find best fleet sizes [5] and even to decide best layout topology to minimize traffic and delay etc. [6, 7]. Since the demand for operations equipments varies over the time due to number of ships that are being serviced at a port in any given time interval, optimal number of operation equipments needed also varies with time. Therefore this research is focusing on deciding the best fleet size once layout of the CT is evaluated for efficient operations. Rest of the paper is arranged as follows: section 2 presents the methodology and the respective mathematical models adapted in the research. Case study is presented in Section 3 and results are given in section 4. This is followed by conclusion and discussion in section 5.

2. Methodology

The methodology proposed in this paper is two folded. In the first stage, given layout of the CT is evaluated for overall operational efficiency analytically and perform necessary changes to the layout and tested new layout in simulation model using Arena simulation package. In the second stage, best prime mover fleet size is decided for the modified layout of the CT by analytical mode and later validates it using Arena simulation package.

2.1 Stage 1: Finding the optimum layout from the given layout

The layout of the flow path can be designed in various ways, initially the facility layout, the layout of the flow path and the location of pick-up and delivery points can be determined simultaneously. Secondly, the design of the flow path and the location of pick-up and delivery points can be determined by considering the layout of the facility as an input factor. Finally the flow path can be designed, considering the layout of the facility and the location of pick-up and delivery point. In order to reduce the cost of operation, the no of shifts as well as fuel usage should be kept at a minimum. For increase the efficiency of the layout, the ship delay should be minimized. [8]

\[
\text{Ship Time} = (\text{sum of loading and unloading time}) + (\text{slack time of the QC}s)
\]

Therefore, it is essential to minimize the total transportation time between the QC and storage location.

Figure 1: The interaction between Container Terminal processes

Arrival of vessel → Loading and unloading of vessel → Transport of container → Storage of containers in the storage yard

Loading

→ Unloading

Customer Retrieval

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Figure 2: Given layout

Figure 3 : Graph representation of the container terminal problem. Ship nodes are denoted $s = 1, \ldots, S$, position nodes $p = 1, \ldots, P$ and vehicle nodes are denoted $v = 1, \ldots, V$. A set of directed arcs connect all ships with all positions and, correspondingly, a set of directed arcs connect positions with vehicles. All positions within each block are connected with directed arcs. The illustrated graph is repeated for each container $c$, including only the ship and vehicle nodes, compatible with $c$.

Assumptions considered are: Only one ship is considered for allocation, All prime movers operate at the same speed, The ship length is negligible (the storage location in the yard has the same distance from any of the QCs), Loading cannot start until unloading of the ship is completed, Loading/unloading sequence and the storage location in the yard are predetermined.
The objective function is to minimize the total transportation time for containers through the terminal. \( \sum_{c \in C, c \in (SUP), i \in (PUV)} T_{ij} \)  

Where, \( c = \{1, 2, 3, \ldots, C\} \) containers, \( s = \{1, 2, 3, \ldots, S\} \) container ships \( p = \{1, 2, 3, \ldots, P\} \) positions in the yard, \( v = \{1, 2, 3, \ldots, V\} \) prime movers \( A, s \in C \): arrival time for ship \( S \), \( D_v \), \( v \in V \) departure time for vehicle \( V \), \( T_{ij} \), \( i \in SUP, j \in PUV \) transportation time between nodes \( i \) and \( j \) \((i \neq j) \), \( x_{cij} \) 1 if container \( c \) is moved directly from node \( i \) to \( j \) 

2.2 Step 2: Designing the optimal number of prime movers for a Container Terminal 

Number of assumptions were considered in this stage also: only unloading process is taken in to account during the simulation, four separate cyclic paths considered there are four queues of unlimited number of transporter vehicles in front of each and each path. (But due to limitations in students version this number is taken as 100), Loading time near a QC is considered as a constant value for each and each path. These values differ from path to path but same for the transporters in a one particular path. Unloading time near a stacking crane is considered as a constant value for each and each path. These values differ from path to path but same for the transporters in a one particular path, Delays caused due to traffic congestion are considered as a constant value for each and each path. These delays differ from path to path but same for the transporters in a one particular path, Transporters are assumed to have a one particular speed when they’re loaded and comparably higher speed when they travel freely 

In order to find the best feet size of prime movers for the above proposed layout, a simplified version of the layout design is considered and it is converted into a network diagram, it is shown in Fig 5.
Where Q1, Q2, Q3 are Quay cranes of the terminal, 1, 2, 3 and 4 are stacking stations, and L - Path of loaded prime movers and E - Path of emptied prime movers, Li,j - Path of prime movers with loads of ith Quay crane to the jth station Where; 1 ≤ i < 4 and 1 ≤ j < 5

\[
\begin{bmatrix}
L_{1,1} & L_{1,2} & L_{1,3} & L_{1,4} \\
L_{2,1} & L_{2,2} & L_{2,3} & L_{2,4} \\
L_{3,1} & L_{3,2} & L_{3,3} & L_{3,4} \\
L_{4,1} & L_{4,2} & L_{4,3} & L_{4,4}
\end{bmatrix}
\]

There is a matrix for a unloading path as well.

Mathematical equations were developed for the vehicle operations for material handling in container terminals. The time for a typical delivery cycle in the operation of a vehicle transport system consists of (1) loading at the pickup station, (2) travel time to the drop off station, (3) unloading at drop-off station and (4) empty travel time of the vehicle between distances

**Cycle time per delivery (T_{i,j})** is given by

\[
T_{i,j} = T_{L} + \frac{L_{i,j}}{V_{i}} + T_{U} + \frac{L_{i,j}}{V_{e}}
\]

Where, \(T_{L}\) - cycle time of a prime mover with loads of ith QC to the jth station, \(T_{U}\) - time to load at a QC, \(L_{i,j}\) - distance between ith QC and jth station unloading point, \(V_{i}\) - Velocity of the prime mover once it is been loaded, \(T_{U}\) - Time to unload at a stacking crane, \(L_{i,j}\) - Distance between jth station and ith QC, \(V_{e}\) - Velocity of the prime mover once is been unloaded

**Total cycle time per delivery (T_{e})** is given by

\[
T_{e} = \sum_{i=1}^{4} \sum_{j=1}^{4} n_{i} C_{i,j}
\]

Where, \(n_{i}\) - jobs handled by the ith QC, \(C_{i,j}\) - cycle time per delivery. The total cycle time can be used to determine certain parameters of interest in the vehicle based system such as Rate of deliveries per vehicle and Number of vehicles required to satisfy a specified total delivery requirement.

**The hourly rate of deliveries per vehicle (H_{ij})** is

\[
H_{ij} = \frac{60 \text{ minutes}}{T_{ij}}
\]

Adjusting of any time losses during the hour should be taken in to account. Possible time losses are availability (reliability factor), Traffic congestion, Efficiency of prime movers

**Available time (AT)** is \(AT = 60 \times AT \times E\)

Where, \(A\) - Availability factor, \(T\) - Traffic factor to indicate traffic congestion, \(E\) - Worker efficiency, now the hourly rate of deliveries equation can be modified as follows

**The hourly rate of deliveries per vehicle (H_{ij})** is

\[
H_{ij} = \frac{AT}{T_{ij}}
\]

**Optimal number of vehicles (N_{e})** needed to satisfy a specified flow rate of deliveries in the system can be estimated by dividing the total workload by available time per vehicle.

\[
N_{e} = \frac{W}{AT}
\]
Workload \( (W_L) \) is given by,
\[
W_L = R_F T_d
\]

Where, \( R_F \) - Specified flow rate of total deliveries for a system (delivery/hour), \( T_d \) - Delivery cycle time (minutes/delivery)

Therefore, \textbf{Optimal number of vehicles} \( (n_C) \) is,
\[
n_C = \frac{R_F}{R_d}
\]

Where, \( R_F \) - Specified flow rate of total deliveries for a system (delivery/hour), \( R_d \) - Hourly rate of deliveries per vehicle

\textbf{3. Case study}

A case study has been carried on the given layout, considering the critical factors best optimal layout is created (Figure 6).

![Figure 6: Modified version of the layout](image)

\textbf{3.1 Analysis and evaluation of performance of the Container Terminal on modified layout}

![Figure 7: Analysis and evaluation of performance of the Container Terminal on modified layout](image)
Here the optimal paths and minimum distances for each block can be defined, for an instance optimal path for blocks 5, 6, 7 paths and distances are given in Table 1. But, if there is traffic on transportation, the next best alternative paths are to be considered.

<table>
<thead>
<tr>
<th>Block number</th>
<th>Path</th>
<th>Distance</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>S1-P1-P2-P6-P5</td>
<td>d1+6d2+2d3+d4+d5</td>
</tr>
<tr>
<td>6</td>
<td>S1-P1-P2-P3-P7-P6</td>
<td>d1+8d2+3d3+d4+d5</td>
</tr>
<tr>
<td>7</td>
<td>S1-P1-P2-P3-P4-P8-P7</td>
<td>d1+9d2+4d3+d4+d5</td>
</tr>
</tbody>
</table>

Simulation of the CT was done with traffic rules for prime movers and without traffic rules. The simulation model consists of ship arrival to berth, quay crane process, process flow of hazardous area, cooling area, regular area and export area sub modules. Simulations were carried out for several times with different batches and value added time, waiting time and total times were measured for all batches with and without traffic rules. In addition, above time measurements were calculated for ships and prime movers separately. In this stage one quay crane and for four stacking stations are modelled in the Arena software. Container allocation for QC’s was modelled as given in the variation of Figure 6. Mainly two scenarios considered.

In the first scenario we have compared the effect of traffic congestion on the optimal number of vehicles that are to be assigned to each and every considered path. A,
4. Results
Simulation of the CT was done with traffic rules for prime movers and without traffic rules. The simulation model consists of ship arrival to berth, quay crane process, process flow of hazardous area, cooling area, regular area and export area sub modules. Simulations were carried out for several times with different batches and value added time, waiting time and total times were measured for all batches with and without traffic rules. In addition, above time measurements were calculated for ships and prime movers separately. These results are presented in Table 2 and Figure 8 and Figure 9.

<table>
<thead>
<tr>
<th>Entity</th>
<th>Value added time/mins</th>
<th>Wait time/mins</th>
<th>Total time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Without traffic rule</td>
<td>With traffic rule</td>
<td>Without traffic rule</td>
<td>With traffic rule</td>
</tr>
<tr>
<td>Trucks</td>
<td>15.0489</td>
<td>17.7651</td>
<td>17.4135</td>
</tr>
<tr>
<td>Ships</td>
<td>512.03</td>
<td>700.45</td>
<td>485.56</td>
</tr>
<tr>
<td>Total</td>
<td>910.16</td>
<td>523.87</td>
<td>875.40</td>
</tr>
</tbody>
</table>

Table 2: Simulation results for the layout 5

This clearly shows that for a traffic congestion situation the modified layout gives the optimum results, hence it is more efficient. The next step is to find the optimum no of prime movers for the modified optimum layout in order to achieve higher efficiency.

![Comparison of the effect of traffic on the jobs being served in path A (Traffic congestion is considered, \( T_f = 0.95 \)](image)

Figure 8: Comparison of the effect of traffic on the jobs being served in path A (Traffic congestion is considered, \( T_f = 0.95 \))

This clearly shows the effect of the traffic congestion on the jobs being served and the number of prime movers that are to be applied to path ‘A’. Here we can observe that the jobs are being more efficiently served when there is no
traffic (Obvious truth). However we can see that as the number of prime movers loaded at the QC increases the jobs delivered to the stacking yard are significantly decreasing when there is traffic.

In addition to above parameters prime mover acceleration and deceleration, break downs, accidents etc. are other parameters what determines the efficiency of the operation. Specified flow rate of total deliveries for a system is the other crucial parameter that determines the efficiency of the operation. Since we have considered a single cargo carrier problem we outrun the possibilities of fluctuating supplies.

![Figure 9: Comparison of the vehicles left from loading station and vehicles reached to the unloading station](image)

5. Discussion and Conclusion

In this research we tried to investigate the factors that are associated with the layouts to improve the productivity of the container terminals. The summarized results shows that it is needed to consider the traffic congestion and minimum distance paths to achieve the high productivity of the container terminal. According to the sizes of the seaport material handling equipments and travelling paths, marshalling area should be arranged to improve the efficiency. In order to minimize re-handling time and traffic congestion it is compulsory to have a pre determined careful planning of storage locations. The distance of path and the velocities of prime movers are the main parameters that determine the prime mover cycle time. Therefore the number of prime movers that are sent after loading (near QC) can be considered as essential.

References

8. Andy King-sing Wong, Minfo tech, GradDipCompSc(Queens land University of Technology) Bsc, CertEd (University of Hong Kong), April 2008, Optimization of container process at Multimodal Container Terminal.